Li^(p)-service? An algorithm for computing p-adic polylogarithms

Coleman defined p-adic analogues of the complex polylogarithms in "Dilogarithms, regulators, and p-adic L-functions", $Invent.\ Math.$, 69:171–208, 1982. We describe an algorithm for computing these p-adic polylogarithms up to a given precision.