

# A Modeling Framework for Gossip-based Information Spread

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**Abstract**—We present an analytical framework for gossip protocols based on the pairwise information exchange between interacting nodes. This framework allows for studying the impact of protocol parameters on the performance of the protocol. Previously, gossip-based information dissemination protocols have been analyzed under the assumption of perfect, lossless communication channels. We extend our framework for the analysis of networks with lossy channels. We show how the presence of message loss, coupled with specific topology configurations, impacts the expected behavior of the protocol. We validate the obtained models against simulations for two protocols.

## I. INTRODUCTION

Gossip protocols have emerged as an attractive solution for distributing information in large-scale systems, due to their simplicity and efficiency. Randomness and the distributed nature of gossip protocols considerably increase their robustness compared to deterministic protocols, also in the presence of failures and data loss.

Although gossip protocols are characterized by their superficial simplicity, the large-scale behavior of a gossip system is not easily predictable. From the perspective of protocol design and behavior prediction, this is an undesirable situation, and with the growing number of gossip protocols, there is an increasing demand for their analysis in an insightful and systematic way.

However, the formal analysis of these protocols is still a rather unexplored research field with many challenges, in part caused by the fact that traditional techniques quickly lead to a state-space explosion (see, e.g., [1], [2]). In [3], we have proposed a modelling framework for gossip-based information dissemination protocol, in which each node periodically selects a random peer and shuffles its local data. In this paper, we show that this approach is generally applicable to gossip protocols for information dissemination, and we extend the analysis method to networks with lossy channels. An exchange of data between nodes is modelled as a state transition capturing the presence or absence of a selected data item before and after a gossip between two nodes.

Our modelling framework allows for the prediction of the system behavior in large-scale environments. We propose a model based on local pairwise interactions which in combination with model checking (cf. [4]) or with the mean-field framework (cf. [5]) allows for the analysis of the emergent behaviour of the system. The model can also be used for optimization of system parameters and performance (cf. [3]), and for fast event-based simulation, as it is done in this paper.

We introduce our theoretical framework initially assuming

no communication failures in the network. Later, we show that the framework is applicable to networks where nodes communicate over an unreliable medium. An important part of our proposed framework is the probability  $P_{drop}$  that an observed item in a node's local storage has been replaced by another item after a gossip. We derive the expressions for this probability under the assumption of perfect communication medium for two protocols, Newscast [6] and Shuffle [7]. In the presence of message loss, however, the dependence of the probability on the type of underlying network graph emerges. We deconstruct the expression for  $P_{drop}$  into its main components, and identify the ones that depend on specific scenario configurations, i.e., message loss and topology combinations. One such component is the probability of an observed item found at one gossiping node, to be also found at its peer. Since it is not feasible to cover all possible network topologies in one formula, the computation of this probability is based on statistical data that can be obtained from Monte Carlo simulations of the protocol at hand.

Since the work of Demers et al. [8], gossip protocols often follow bidirectional data exchange (push-pull) for better performance. As observed in [9], the performance of these protocols is usually evaluated under the assumption of a perfect, error-free communication medium. Thus, data exchange operations between nodes are generally considered to be atomic operations, e.g., [10], [11], [12], [13], [14], [7], [15], [3]. That is, if a node initiates a gossip with another node, both nodes base their local decisions upon each other's data, and in some protocols even guarantee the preservation of each other's data. In practice, however, implementing data exchange as an atomic operation is hard to achieve assuming communication over unreliable media [16].

In this respect, our paper makes an additional contribution; it investigates the impact of a realistic environment with lossy communication channels on a push-pull-based gossip protocol. Furthermore, we present in more detail the following observations: (a) Introducing message loss in the network model affects the emergent behavior of the protocol in a specific manner: with the introduction of lossy communication channels, the correlation between local storage content of neighboring nodes increases, and the degree of the correlation depends on the network topology. (b) The fewer neighbors nodes have in the underlying network, the stronger the effect of message loss on the emergent behavior of the protocol. For fully connected networks, message loss does not have an impact on the distribution of data over the network, which

remains uniform (as observed when there are no losses).

Two areas of research are relevant to our work: generic modelling frameworks for gossip protocols and the performance of gossip protocols in the presence of message loss. Automated mean-field framework for dynamic gossip networks has been presented in [17]. Due to the underlying mean-field method, used by this framework, the results are accurate only for very large networks and for average behavior of the modelled system. The mean-field framework can be combined with our framework, as it is shown in [5] for Shuffle.

There is previous work [18] on a simple gossip-based membership protocol with nonatomic protocol actions in the presence of message loss of up to 1%. The authors proposed to use a push-based gossip protocol, in which only an active node sends data to its peer, and immediately removes the sent data from its cache. Moreover, the node sends only two items, IP addresses and ports of itself and of a random peer from its local cache. In the protocols that we study, each gossiping pair exchanges a random subset of the data items. The authors show the protocol correctness modelling it by graph transformations, similar to the approach in [2]. The protocol properties analyzed include the expected number of neighbors a node has and the uniformity of the neighborhood lists.

The paper is organized as follows. Sec. II outlines the class of gossip protocols that can be analyzed with our framework, presented in Sec. III. We consider two case studies, Newscast and Shuffle, and demonstrate the modelling and derivation of the state transition matrix for them, in Sec. IV and Sec. V, respectively. In Sec. VI, we model and analyze Shuffle in the presence of message loss. Sec. VII stretches the scope of our theoretical framework to gossip-based membership protocols like Cyclon. Sec. VIII concludes the paper.

## II. BACKGROUND

In this section, we specify a class of gossip protocols for which our modelling framework is applicable. We consider large networks, where nodes interact in a peer-to-peer style. All nodes have a common agreement on the frequency of gossiping. Each node stores local data in its *cache* and executes two different threads, an active and a passive one (see Fig. 1). The active thread periodically initiates a contact with a randomly chosen peer  $p$  by sending it a (sub)set  $\sigma$  of its cache, and waits for a reply. Upon reception of the reply  $\sigma_p$ , the node updates its cache based on the cache,  $\sigma$  and  $\sigma_p$ .

The passive thread waits for a message sent by the active thread of a neighbor and replies to it with its data  $\sigma$ . The node then updates its cache based on the stored, received and sent data. The message with its content is called an *exchange*

<pre> <b>wait</b> (<math>\Delta t</math> time units) <math>p \leftarrow \text{RandomPeer}()</math>; <math>\sigma \leftarrow \text{PrepareMsg}()</math>; <b>send</b> <math>\sigma</math> to <math>p</math>; <b>wait until</b> receive(<math>\sigma_p</math>) <math>\sigma \leftarrow \text{Update}(\sigma, \sigma_p)</math>; </pre>	<pre> <b>wait until</b> receive(<math>\sigma_p</math>) <math>\sigma \leftarrow \text{PrepareMsg}()</math>; <b>send</b> <math>\sigma</math> to sender(<math>\sigma_p</math>); <math>\sigma \leftarrow \text{Update}(\sigma, \sigma_p)</math>; </pre>
(a) active thread	(b) passive thread

Fig. 1. Skeleton of a gossip protocol

*buffer*. Nodes that execute their active thread are *initiators*, and nodes that execute their passive thread are called *contacted*.

The generic protocol, described above, is a *push-pull* gossip protocol. Other variations of gossip protocols are ones in which the initiator only sends local data to its gossip partner (*push*), and ones in which an initiator only requests data from its peer (*pull*). All three versions of gossip protocols are covered by our framework.

The random peer selection `RandomPeer()` is based on the set of neighbors as determined by the underlying network graph. The nature of the data and the result of the generic operations in Fig. 1 are application-dependent. In gossip-based information dissemination protocols like [13], [7], a finite list of news items composes the local cache of a node. The operation  $\sigma \leftarrow \text{PrepareMsg}()$  in Fig. 1 selects a random (or predefined) set of items from the cache of the node. The method `Update` merges the list of old items with the list of received items. Properties of the protocols that can be analyzed within our framework include the number of copies of an item in the network over time and the speed at which items spread throughout the network.

In gossip-based membership management protocols such as [14], [19], a cache of each node consists of a set of its peer IP addresses, called the *partial view* of the membership of the network. `Update` produces a sample of the union of the old and the received views. The performance metrics of these protocols include a distribution of the partial view size, and the number of nodes reached in the presence of node failures.

We refer to [20] for other applications of gossip protocols. As we demonstrate later in this paper, our framework models gossip-based information dissemination protocols, but it can be also applied to other type of applications, such as gossip-based membership protocols.

## III. PAIRWISE INTERACTION MODEL

An exchange of data items between nodes is modelled as a state transition, capturing the presence or absence of an observed data item  $d$  before and after a gossip interaction between *two nodes: an initiator A and a contacted node B*. Each state is then a pair  $(a, b)$  of bits, each indicating the presence (if equal to 1) or the absence (if equal to 0) of the item in the cache of  $A$  and  $B$ , respectively.

The model has four possible states of the caches of  $A$  and  $B$ : (1) when both hold  $d$ , (2–3) either of the caches holds the item  $d$ , and (4) neither cache holds  $d$ . These correspond to the states  $(0, 0)$ ,  $(0, 1)$ ,  $(1, 0)$ , and  $(1, 1)$  in the state transition diagram, shown as Fig. 2. Transitions from one state to another are labelled by the respective transition probabilities  $P(a_2 b_2 | a_1 b_1)$ , where  $a_1 b_1$  is the state before a gossip interaction, and  $a_2 b_2$  is the state after the interaction, with  $a_i, b_i \in \{0, 1\}$ .  $a_1, a_2$  and  $b_1, b_2$  correspond to states of nodes  $A$  and  $B$ . For instance,  $P(01|10)$  means that node  $A$  had  $d$  before the interaction, which it passed on to  $B$ , afterwards.

The building blocks of all transition probabilities  $P(a_2 b_2 | a_1 b_1)$  of the state diagram are two probabilities: (i) the probability  $P_{select}$  of an item to be selected by a node

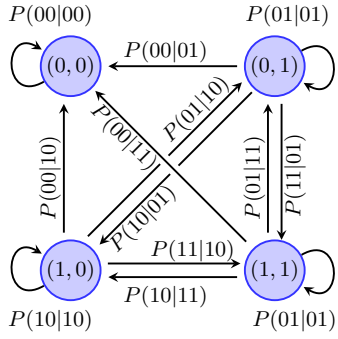


Fig. 2. Pairwise interaction model

from its cache for a gossip, and (ii) the probability  $P_{drop}$  that an item is replaced by another one, received by its node in the gossip. The expressions for  $P_{select}$  and  $P_{drop}$  depend on specifics of the operations PrepareMsg and Update, respectively. Moreover, these probabilities are functions of the number of items  $n$ , exchange buffer size  $s$ , and cache size  $c$ , and  $0 < s \leq c$ . We assume that  $c < n$ , i.e. all  $n$  items cannot be stored in a single local cache. We explain our framework by considering state transitions and computing the corresponding probabilities for several case studies.

Our state diagram differs from a Markov chain of the system: it expresses a state of gossiping pair rather than state of all nodes. The transition probabilities are used with other frameworks, e.g., mean-field framework and numerical simulations, to study the emergent behaviour of system.

#### IV. CASE STUDY: NEWSCAST

We now briefly describe our first case study, a simple push-pull information propagation protocol. It is a variation of the Newscast protocol [6]. In the original Newscast, each item is paired with a timestamp indicating when it was created. This protocol can also be modelled using our analytical framework; we will come back to the details in Sec. VII.

The basic idea of the protocol is a periodic exchange of data items published by nodes in the network. Items can be, for example, a number or network address (IP and port) of a node. For now, we assume that nodes do not crash and communication channels are failure-free.

##### A. Specification

The protocol operates in a wide area network<sup>1</sup>. A node periodically picks a random peer and exchanges  $s$  random items with it. The node then selects  $c$  random items for its new cache among the received items and those in its cache. The methods in Fig. 1 for Newscast are summarised in the following table:

method	operation
RandomPeer()	select a peer uniformly at random
PrepareMsg()	select $s$ random items
Update( $\sigma, \sigma_p$ )	store only $c$ random items, selected among the items in its cache and the received items $\sigma_p$

<sup>1</sup>In the network of gossiping nodes, an information dissemination is fully dictated by gossiping frequency instead of communication latencies (cf. [6]).

##### B. Transition diagram

We analyse the spread of a generic item, which we call  $d$ , using the framework introduced in Sec. III. As stated previously, there are four possible states of the caches of  $A$  and  $B$ . The state  $(0, 0)$  has only one outgoing transition, back to itself.  $P(00|00) = 1$  since if  $A$  and  $B$  do not have  $d$  before their exchange then they clearly still do not have  $d$  after the exchange. We now determine values for other probabilities  $P(a_2b_2|a_1b_1)$ . Due to the symmetry of exchange between gossiping nodes in the protocol,  $P(a_2b_2|a_1b_1) = P(b_2a_2|b_1a_1)$ , and  $P_{drop}$ ,  $P_{select}$  are the same for active and passive nodes. We use  $P_{-select}$  for  $1 - P_{select}$ , and  $P_{-drop}$  for  $1 - P_{drop}$ .

**State  $(0, 1)$ .** Before gossip,  $d$  is only in the cache of node  $B$ .  
 $a_2b_2 = 01$ :  $B$  neither sends nor drops  $d$  from its cache, or  $B$  sends and keeps  $d$ , and  $A$  drops it, i.e., the probability is  $P(01|01) = P_{-select} \cdot P_{-drop} + P_{select} \cdot P_{-drop} \cdot P_{drop}$ .  
 $a_2b_2 = 10$ :  $B$  selects and drops  $d$ , and  $A$  keeps it; i.e., the probability is  $P(10|01) = P_{select} \cdot P_{drop} \cdot P_{-drop}$ .  
 $a_2b_2 = 11$ :  $B$  sends  $d$ , and both nodes keep it; i.e.,  $P(11|01) = P_{select} \cdot P_{-drop} \cdot P_{-drop}$ .  
 $a_2b_2 = 00$ :  $B$  sends  $d$  and both nodes drop it, or  $B$  does not send and drops  $d$ ;  $P(00|01) = P_{select} \cdot P_{drop} \cdot P_{drop} + P_{-select} \cdot P_{drop}$ .

**State  $(1, 1)$ .** Before gossip,  $d$  is in the caches of both nodes.  
 $a_2b_2 = 01$ : node  $A$  drops  $d$  while updating its cache, but  $B$  keeps it; i.e.,  $P(01|11) = P_{-drop} \cdot P_{drop}$ .  
 $a_2b_2 = 10$ : this transition is symmetric to the previous one.  
 $a_2b_2 = 11$ : neither  $A$  nor  $B$  drops the item  $d$ ; i.e.,  $P(11|11) = (P_{-drop})^2$ .  
 $a_2b_2 = 00$ : both  $A$  and  $B$  drop  $d$ ; i.e.,  $P(00|11) = (P_{drop})^2$ .

All transition probabilities are summarized in Fig. 3

$P(01 01) = P(10 10) = (P_{-select} + P_{select} \cdot P_{drop}) \cdot P_{-drop}$		
$P(10 01) = P(01 10) = P_{select} \cdot P_{drop} \cdot P_{-drop}$		
$P(11 01) = P(11 10) = P_{select} \cdot P_{-drop} \cdot P_{-drop}$		
$P(00 01) = P(00 10) = (P_{select} \cdot P_{drop} + P_{-select}) \cdot P_{drop}$		
$P(01 11) = P(10 11) = P_{-drop} \cdot P_{drop}$		
$P(11 11) = (P_{-drop})^2$	$P(00 11) = (P_{drop})^2$	$P(00 00) = 1$

Fig. 3. Transition probabilities

##### C. Building blocks: $P_{select}$ and $P_{drop}$

We now derive the expressions for the probabilities  $P_{select}$  and  $P_{drop}$ . The following analysis assumes that all node caches are full; that is, the network is already running for a while.

Consider nodes  $A$  and  $B$  engaged in an exchange, and let  $B$  receive the exchange buffer  $S_A$  from  $A$ . Let  $k$  be the number of duplicates (see Fig. 4), i.e., the items of an intersection of the node cache  $C_B$  and the exchange buffer of its gossip partner  $S_A$  (i.e.,  $S_A \cap C_B$ ).

The probability of selecting an item  $d$  in the cache is the number of selected items  $s$  divided by the total number of items in the cache  $c$ :  $P_{select} = \frac{s}{c}$ . Thus, the probability that an item  $d$  in the cache is not selected is:  $P_{-select} = \frac{c-s}{c}$ .

Among the  $c$  items in  $C_B$ , there are  $k$  items also in  $S_A$ ; thus, only  $c$  random items of the total  $c + s - k$  items in

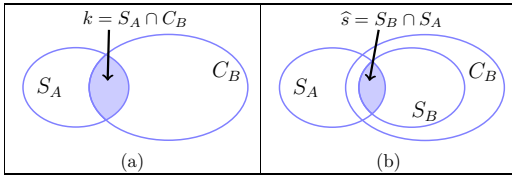


Fig. 4. a) Items sent by  $A$  that are in the cache of  $B$ ; b) Items in common for the exchange buffers of both  $A$  and  $B$ .

$C_B \cup (S_A \setminus C_B)$  can be kept:  $P_{\neg drop}(k) = \frac{c}{c+s-k}$ . Thus, the probability  $P_{drop}$  that an item in  $C_B \cup (S_A \setminus C_B)$  is dropped from  $C_B$ , given  $k$  items in  $S_A \cap C_B$  is as follows:

$$P_{drop}(k) = 1 - \frac{c}{c+s-k}. \quad (1)$$

Assuming uniform sampling of items, the average value of  $k$  is  $s \cdot \frac{c}{n}$ . Thus, the probability of dropping an item after the exchange  $P_{drop}$  is  $\frac{1}{1+cn/(s(n-c))}$ . Later we discuss a case when the assumption of uniform sampling does not hold.

#### D. Validation

To validate our theoretical results, we simulated Newscast in a round-based fashion similar to simulations in PeerSim [21]. A new item  $d$  is initially introduced in a network of 2500 nodes at one node. In this fully connected network, caches of all nodes are full and uniformly populated by  $n = 500$  items. After each gossip round, we measure the total number of copies of  $d$  in the network (*replication* property), and how many nodes in total have seen  $d$  over time (*coverage* property).

*Simulations with the simplified Newscast:* Each node in the network has a cache size of  $c = 100$ . Once in a round, every node selects uniformly at random one node from the network of 2500 nodes and exchanges  $s = 50$  random items. For a fair comparison with the simulations with the model, we let the nodes gossip for 1000 rounds items other than  $d$ ; items are replicated and the replicas fill the caches of all nodes. At the round 1000, the observed item  $d$  is inserted into the network at a random location. From that round on, replication and coverage are measured by the end of each round.

*Simulations with the model:* For the simulations with the model, the system parameters  $n, c$  and  $s$  are set to 500, 100 and 50, respectively. Each node in the network only maintains a state variable which indicates the presence or absence of  $d$ . Nodes update their state in pairs according to the transition probabilities in Fig. 3. While in the actual protocol, nodes update the contents of their caches, in the model simulations, nodes update only their state variables. Since we do not need a startup time for the simulations with the model, at the round 0, we set the state of a random node to 1, and all others to 0. From that round on, we track the states of the nodes.

The graphs in Fig. 5 depict the performance of the simplified Newscast and of the analytical model in terms of replication (left) and coverage (right) of  $d$ . The results are collected from 1000 simulation runs of the protocol and 1000 runs of the model. In approximately 72% of the all runs, the observed item disappears. In the graphs, however, we only considered the runs where the item did not disappear; e.g., to obtain 1000

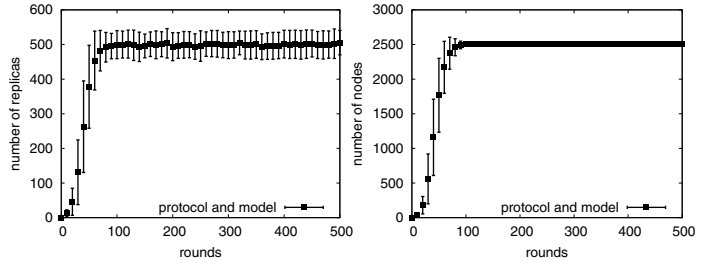


Fig. 5. **Clique:** Replication (left) and coverage (right) of item  $d$  for Newscast and its model, with  $c = 100$ ,  $n = 500$ ,  $s = 50$ .

runs of the protocol displayed in Fig. 5, we performed a total of 3700 runs. Assuming a normal distribution of the results, the confidence interval for 95% confidence is 16 times narrower than the standard deviations drawn on the graphs.

Fig. 5 show the average and standard deviation of the successful runs with Newscast. The standard deviation bars on the graphs are the standard deviation of the replicas and number of nodes that have seen item in the system. For all successful runs, the network reaches the equilibrium, in which there are around 500 replicas of  $d$ . Due to random gossiping, item  $d$  is eventually seen by all nodes in the network, when coverage reaches all 2500 nodes.

We have chosen this type of network graph for a basic introduction of our framework since a uniform distribution of items over the network is clearly a valid assumption in a fully connected network of nodes executing Newscast. We will turn to other types of network graphs in the next case study. Our framework allows for modelling of push-only as well pull-only gossip protocols, see [22].

## V. CASE STUDY: SHUFFLE

We now move on to another case, the Shuffle protocol introduced in [7] and originally analyzed in [3] using our framework. This section is intended to make the reader familiar with the analysis of this protocol.

#### A. Specification

Shuffle aims at the conservation of data in an ad hoc network. Each node maintains a cache of data items that are disseminated throughout the network. The dissemination is done by periodic exchange of  $s$  random items between two gossiping peers. The generic routines in Fig. 1 can be summarized for Shuffle as follows:

method	operation
RandomPeer()	select a peer uniformly at random
PrepareMsg()	select $s$ random items
Update( $\sigma, \sigma_p$ )	<ul style="list-style-type: none"> <li>• add <math>\sigma_p</math> received entries to the cache;</li> <li>• remove duplicated items;</li> <li>• remove items among <math>\sigma \setminus \sigma_p</math> uniformly at random until the cache has <math>c</math> items.</li> </ul>

The procedure of selection of items is similar to the one in Newscast, but items are discarded according to a different policy: (i) a node cannot discard an item unless it is sent to the gossip partner; (ii) the partner is not allowed to drop received items. A node can keep only  $c$  items in its cache after the exchange. A peer will favor dropping items it has just sent over other items in its cache. Note that in this way, an exchanged

item will always be preserved, and possibly even replicated. Thus, discarding items does not lead to the loss of information in the network (if there is no message loss).

### B. Transition Diagram

Unlike in Newscast, nodes are not allowed to discard the items received from their gossip partners. Taking this difference into account, the transition probabilities for Shuffle are quite easy to derive from the transitions in Fig. 3. Note that for this protocol the state  $(0, 0)$  has only a self-transition, and no other outgoing or incoming transitions, because of the preservation nature of the protocol. That is, if either nodes send an item, its partner keeps this copy as well, and if an item is not among the selected for a shuffle, the item is not replaced by another one. The transition probabilities can be easily computed, see Fig. 6. For more details on derivation of these transition probabilities, we refer to [3].

$$\begin{aligned} P(01|01) &= P(10|10) = P_{\neg select} & P(10|01) &= P(01|10) = P_{select} \cdot P_{drop} \\ P(01|11) &= P(10|11) = P_{select} \cdot P_{\neg select} \cdot P_{drop} & P(00|00) &= 1 \\ P(11|10) &= P(11|01) = P_{select} \cdot P_{\neg drop} \\ P(11|11) &= 1 - 2 \cdot P_{select} \cdot P_{\neg select} \cdot P_{drop} \end{aligned}$$

Fig. 6. Transition probabilities for Shuffle

$P_{select}$  remains the same as for Newscast,  $\frac{s}{c}$ . However,  $P_{drop}$  is different for Shuffle, and we derive it in the next section.

### C. Probability of Dropping an item

$P_{drop}$  represents the probability that an item that can be overwritten is indeed overwritten by an item received by its node in the exchange.  $P_{drop}$  depends on the number of items both gossiping nodes have in common, in particular, how many of such items the contacted node receives during the exchange. To derive the expression for  $P_{drop}$ , we assume a uniform distribution of items over the network; in the absence of message loss, this assumption is supported by experiments in [7], [23], [3] and analysis in [24].

Consider again Fig. 4. By assumption,  $C_A$  and  $C_B$  are a uniform selection from the entire population of  $n$  items.  $S_A$  and  $S_B$  are chosen uniformly at random from  $C_A$  and  $C_B$ , respectively. After the exchange, node  $B$  has to allocate items from  $S_A$  in its cache  $C_B$ , taking into the account the duplicated items in  $S_A \cup C_B$  and  $S_A \cup S_B$ . Basically, the items in  $S_B$  that are not in  $S_A$  are replaced by items in  $S_A$  that are not in  $C_B$ . So, every item from  $S_A \setminus S_B$  that is in  $C_B$  means that one item from  $S_B \setminus S_A$  can be kept in  $C_B$ . In other words, the probability  $P_{drop}$  that an item from  $S_B \cup S_A$  is dropped from  $C_B$  equals to the probability that an item from  $S_A \setminus S_B$  is not in  $C_B$ . By uniform distribution, the probability is  $\frac{n-c}{n-s}$ . Thus,  $P_{drop} \approx \frac{n-c}{n-s}$ . This approximation of  $P_{drop}$  for Shuffle has been successfully established through experiments [3], and used for modelling and optimization in [3], [4].

## VI. SHUFFLING THROUGH LOSSY CHANNELS

So far, the analysis has relied on the assumption that nodes interact in a perfect, lossless communication environment. We now consider ad hoc networks where nodes are continually

communicating with each other over an unreliable medium. We now explore the impact of lossy channels on a gossip protocol with a push-pull information exchange.

### A. Assumptions

Every message sent now has a fixed, positive probability to be lost due to a disturbance of the communication medium. As explained in the introduction, we no longer assume that the shuffle procedure is atomic.

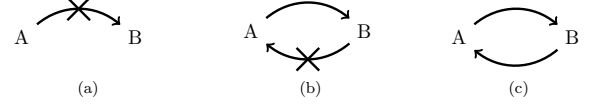


Fig. 7. Scenarios of communication with lossy channels: (a) loss of the request message, (b) loss of the reply message, (c) gossip without loss.

There are three general cases in pairwise communication with respect to message delivery, as depicted in Fig. 7: (a) node  $A$  initiates a gossip with  $B$  by sending a message, but the message is lost, (b) node  $A$  successfully initiates a gossip with  $B$ , but a message from  $B$  is lost on its way to  $A$ , and (c) a gossiping pair receives messages from each other.

### B. Transitions

We take the analytical model of Shuffle described in Sec. V as starting point. In our current model, the state  $(0, 0)$  is no longer isolated, since there is a possibility to remove the only copy of  $d$  from the cache of the node  $B$ , in the scenario shown in Fig. 7(b). We again express the transition probabilities  $P(a_2b_2|a_1b_1)$  in terms of  $P_{select}$ ,  $P_{drop}$ . To analyze the protocol in the presence of message loss, we introduce into the formal model an additional input parameter, the probability  $P_{loss}$  that a message is not delivered to a node due to channel loss. We use  $P_{\neg loss}$  for  $1 - P_{loss}$ .

**State  $(0, 0)$ .** Before shuffle, neither  $A$  nor  $B$  have  $d$  in their cache.

$a_2b_2 = 00$ : neither  $A$  nor  $B$  have item  $d$  after a shuffle, because neither of them had it in the caches before the shuffle:  $P(00|00) = 1$ .

$a_2b_2 \in \{01, 10, 11\}$ : cannot occur, because none of the nodes have item  $d$ .

**State  $(1, 0)$ .** Before shuffle,  $d$  is only in the cache of node  $A$ .

$a_2b_2 = 01$ : occurs only when both the request of  $A$  and the reply of  $B$  are successful and node  $A$  selects and drops  $d$ :

$$P(01|10) = (P_{\neg loss})^2 \cdot P_{select} \cdot P_{drop}$$

$a_2b_2 = 10$ :  $B$  does not have  $d$  because: (a)  $A$  did not select  $d$ , or (b)  $A$  selected  $d$  but the request message got lost on the way to  $B$ :  $P(10|10) = P_{\neg select} + P_{loss} \cdot P_{select}$ .

$a_2b_2 = 11$ : both nodes  $A$  and  $B$  have a copy of  $d$  because: (a) either both nodes received the gossip messages and  $A$  selected  $d$  and kept it, or (b)  $A$  selected  $d$  and the reply message from  $B$  got lost; that is,  $P(11|10) = (P_{\neg loss})^2 \cdot P_{select} \cdot P_{\neg drop} + P_{\neg loss} \cdot P_{loss} \cdot P_{select}$

$a_2b_2 = 00$ : cannot occur, as  $A$  would only drop  $d$  if it received a reply, which implies that  $B$  would keep  $d$ .

**State (0, 1).** Before shuffle, a copy of  $d$  is only in the cache of node  $B$ .

$a_2b_2 = 01$ : only  $B$  has  $d$  because the message from  $A$  got lost or,  $B$  received the message, and: (a) it did not select  $d$  or (b)  $B$  selected  $d$ , kept it, and reply got lost; i.e. the probability is  $P(01|01) = P_{-loss} \cdot (P_{-select} + P_{loss} \cdot P_{select} \cdot P_{-drop}) + P_{loss} \cdot a_2b_2 = 10$ : both request and reply messages were successfully delivered and  $B$  selected and dropped  $d$ , which amounts to the probability  $P(10|01) = (P_{-loss})^2 \cdot P_{select} \cdot P_{drop}$ .

$a_2b_2 = 11$ : both messages were delivered successfully, and  $B$  selected and kept  $d$ ;  $P(11|01) = (P_{-loss})^2 \cdot P_{select} \cdot P_{-drop}$ .

$a_2b_2 = 00$ : neither of the nodes have  $d$ , because  $B$  selected and dropped  $d$ , but  $A$  did not receive the reply message.  $P(00|01) = P_{-loss} \cdot P_{loss} \cdot P_{select} \cdot P_{drop}$ .

**State (1, 1).** Before shuffle,  $d$  is in the caches of  $A$  and  $B$ .

$a_2b_2 = 01$ : only  $B$  has  $d$  since both messages were successfully received,  $A$  selected and dropped  $d$  while  $B$  did not select it:  $P(01|11) = (P_{-loss})^2 \cdot P_{select} \cdot P_{drop} \cdot P_{-select}$ .

$a_2b_2 = 10$ : only  $A$  has  $d$  since  $B$  selected  $d$ , dropped it, and  $A$  did not select  $d$ :  $P(10|11) = P_{-loss} \cdot P_{-select} \cdot P_{select} \cdot P_{drop}$ .

$a_2b_2 = 11$ : after the shuffle both nodes have  $d$ , because:

- the message from  $A$  did not arrive at  $B$ , i.e.  $P_{loss}$ ; or
- the message from  $A$  was successfully received by  $B$ , but the reply message got lost, and:
  - \*  $A$  did not select  $d$ , while  $B$  (i) did not select  $d$  as well, or (ii) selected and kept  $d$ .  $P_{-loss} \cdot P_{-select} \cdot P_{loss} \cdot (P_{-select} + P_{select} \cdot P_{-drop})$ ; and
  - \* node  $A$  selected  $d$ :  $P_{-loss} \cdot P_{select} \cdot P_{loss}$ ; or

c) both nodes received each other messages, and:

- \*  $A$  did not select  $d$ , while  $B$  (i) also did not select it, or (ii) selected and kept it:  $(P_{-loss})^2 \cdot P_{-select} \cdot (P_{-select} + P_{select} \cdot P_{-drop})$ ; and
- \* (i)  $A$  selected and kept  $d$ , while  $B$  did not select  $d$ , or (ii) both nodes selected  $d$ .  $(P_{-loss})^2 \cdot P_{select} \cdot (P_{-select} \cdot P_{-drop} + P_{select})$ .

Hence,  $P(11|11) = 1 - (2 - P_{loss} \cdot (3 - P_{loss})) \cdot P_{select} \cdot P_{-select} \cdot P_{drop}$ .

$a_2b_2 = 00$ : discarding of an item by both nodes cannot occur.

While  $P_{loss}$  expresses the reliability of the communication channels,  $P_{select}$  and  $P_{drop}$  are derived based on the behavior of the protocol.  $P_{select}$  is again the random selection of items from the cache; an item has  $\frac{s}{c}$  chance of being selected, regardless of message loss. The calculation of  $P_{drop}$  is complex, and we discuss it in the remainder of this section.

### C. The Probability of Dropping an Item

We now analyze how message loss affects one of the building blocks of our model:  $P_{drop}$ . In Sec. V-C, we have already found an expression for  $P_{drop}$  in the case of Shuffle, relying on the assumption of a uniform distribution of items. Here, we revisit  $P_{drop}$  and derive a general formula without making any assumptions about the distribution of items. Later on, we will explore how message loss affects the distribution of items, and will determine that it is the coupling of message loss and the topology of the network that affects  $P_{drop}$ . Having isolated the component of  $P_{drop}$  that is affected by the message

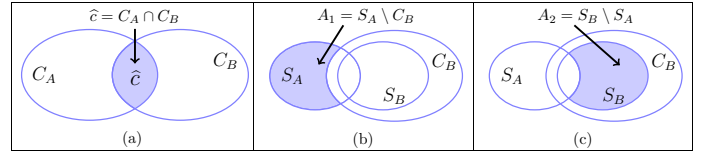


Fig. 8. a) Items in common for the caches of both nodes  $A$  and  $B$ ; b) Items sent by  $A$  that are not in the cache of  $B$ ; c) Items sent by  $B$  that are not in the exchange buffer of  $A$ .

loss/topology coupling, we will propose the use of statistical data to calculate that specific part of the  $P_{drop}$  expression.

When a node selects an item to be sent to a neighbor, there is a probability  $P_{drop}$  that the item will be dropped from the node's cache after the gossip exchange. The selected item may be dropped only when there is a need to create space for an item received from a gossip partner. Therefore, the probability  $P_{drop}$  depends on the relationship between a) the new items received from the gossip partner (for which the node needs space, the shaded area in Fig. 8(b), referred to as  $A_1$ ), and b) the items that the node has selected to send to the gossip partner and is allowed to discard (the shaded area in Fig. 8(c), referred to as  $A_2$ ). In order to find an expression for  $P_{drop}$ , we need to calculate the probability of an item being in  $A_1$  and the probability of an item being in  $A_2$ , which we will denote as  $P(A_1)$  and  $P(A_2)$ , respectively.

Given two nodes,  $A$  and  $B$ , that engage in a gossip exchange, we can represent their caches as sets  $C_A$  and  $C_B$ , and the sets of items they exchange with each other by  $S_A$  and  $S_B$ , respectively. The sets  $C_A$  and  $C_B$  may have common elements (items), see Fig. 8(a). We define  $P_{inx}$  as the probability of any item found in one of the caches to be also found in the other. Knowing  $P_{inx}$ , we can formulate  $P(A_1)$  as  $P_{select} \cdot (1 - P_{inx})$  and  $P(A_2)$  as  $P_{select} \cdot (1 - P_{select} \cdot P_{inx})$ . Thus,

$$P_{drop} = \frac{P(A_1)}{P(A_2)} = \frac{1 - P_{inx}}{1 - P_{select} \cdot P_{inx}} \quad (2)$$

In order to calculate a value for  $P_{drop}$ , it is necessary to have a value for the probability  $P_{inx}$ . For the case of  $C_A$  and  $C_B$  being random samples of a population of  $n$  items, we can analytically deduce that  $P_{inx} = \frac{c}{n}$ . For networks with perfect communication channels, repeated execution of Shuffle results in a uniform distribution of items. In the next section, we look at the effect that lossy channels have on the distribution of items.

### D. Uniform Distribution of Items: Does it Still Hold?

As already mentioned, the calculation of  $P_{drop}$  in the presence of message loss requires us to reason about the contents of the gossip partner's cache. Assuming that the items in the caches of both gossip partners are random samples of the totality of items in the network, we can easily estimate  $P_{inx}$  as  $\frac{c}{n}$  and derive an analytical expression for  $P_{drop} \approx \frac{n-c}{n-s}$ . In this section, we verify whether the uniform distribution of items, observed under no message loss, is still a valid assumption.

### The Importance of Randomness

To understand the effect of message loss on abstract level, consider one node in the network, executing Shuffle. We

examine the scenario from Fig. 7(b), where a reply message from a node to the initiating node is lost due to channel failure. When two nodes  $A$  and  $B$  gossip their local items to each other, the probability that the message from  $B$  to  $A$  is lost, is  $P_{\neg loss} \cdot P_{loss}$ . If the message of  $B$  is not delivered to  $A$ , items  $\hat{c} \cup S_A$  will be common to cache  $C_A$  and cache  $C_B$  after the shuffle, since  $B$ , unaware of the failure, purges the sent items  $S_B$ , and  $A$ , which received no reply, keeps its  $S_A$  items.

Over time neighboring nodes have a growing intersection of items in their cache. If a node has a small neighborhood, the random sample becomes more biased towards the collection of items left in the neighborhood. Limited by the access to the storage space of the neighborhood, a set of neighbors maintains only a subset of all items. For the fully connected graph, since it is the entire collection of the items every node has access to, the uniform distribution assumption in general remains. A larger neighborhood reduces the probability of repeated communication between two nodes, and due to the increased communication range, there is a faster exchange between distant areas of the network.

### Experimental Observations

To support our claims that message loss affects the distribution of items, we conducted simulation experiments. Each experiment has a startup period of 1000 rounds, during which  $N = 2500$  nodes gossip  $n = 500$  different items under no message loss. We use three different network topologies: a fully connected network, a square grid with each internal node having 4 neighbors, and a network where every node has 4 randomly chosen neighbors (outdegree 4). By the end of the startup period, the items have been replicated, achieving uniform distribution. That is, every item has a probability  $\frac{c}{n} = \frac{100}{500} = 0.2$  of being present in a given node's cache. After the startup period has finished, the communication channel is set up to fail with a probability  $P_{loss}$ . We calculate, per round, the probabilities  $P(11)$ ,  $P(10)$  and  $P(01)$  that an exchange involves both nodes having item  $x$ , only the initiator having item  $x$ , or only the gossip partner having item  $x$ , respectively.

Fig. 9 shows the average values of  $P(11)$ ,  $P(10)$  and  $P(01)$  over 1000 rounds for different values of  $P_{loss}$  using the three topologies mentioned earlier. As expected, for the case of no message loss ( $P_{loss} = 0$ ) the probabilities suggest a uniform distribution of items in the network. We can analytically deduce their expected value, which matches the experimental results, with  $P(11)$  as  $\frac{c}{n} \cdot \frac{c}{n} = 0.04$  and  $P(10) = P(01)$  as  $\frac{c}{n} \cdot (1 - \frac{c}{n}) = 0.16$ . However, as the probability of message loss increases, we observe some changes in  $P(11)$ ,  $P(10)$  and  $P(01)$ . For the case of the fully connected network, the probabilities remain stable, suggesting that the uniform distribution of items remains unaffected by message loss. With the other topologies, however, as message loss increases, the number of gossip interactions between nodes that both have item  $x$  also rises. Since item  $x$  is representative of all items in the network, the graphs suggest that, as a consequence of message loss, gossip partners have more items in common than they would have if items were uniformly distributed. In other

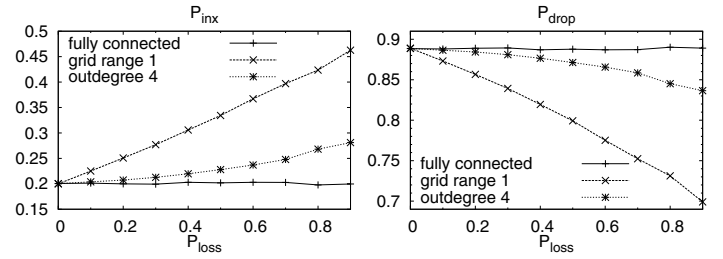


Fig. 10. Probabilities  $P_{inx}$  (left) and  $P_{drop}$  (right), for different topologies.

words, due to message loss, a node is more likely to have items in common with a neighbor than with another random node in the network. Hence, the topology of the underlying network now plays a role in calculating  $P_{drop}$ .

### E. Calculating $P_{drop}$ based on Statistical Data

By now, we have established that in case of message loss the structure of neighborhoods plays an important role in determining the distribution of items, which, in turn, determines the probability of an item found in a node's cache to be also found in the gossip partner's cache,  $P_{inx}$ . Our calculation of  $P_{drop}$  depends on finding a value for  $P_{inx}$ . This topology varying component can be modelled analytically or measured experimentally from a single run of the protocol, for a given topology. Here, we opt for obtaining  $P_{inx}$  for a given network graph from statistical data collected from experiments. With  $P_{inx}$ , we can proceed to calculate  $P_{drop}$ , obtaining the final building block of the model needed for validation. We can calculate  $P_{inx}$  from the probabilities  $P(11)$ ,  $P(10)$  and  $P(01)$  measured experimentally in the previous section:

$$P_{inx} = \frac{P(11)}{P(10) + P(11)}$$

The left graph of Fig. 10 shows the values for  $P_{inx}$  calculated for each experiment using a different  $P_{loss}$ . Based on these values, we compute  $P_{drop}$  using (2), as seen in right graph of Fig. 10. As expected, the calculated values show that, in the face of message loss, different topologies yield different probabilities of dropping an item.  $P_{drop}$  drops more harshly in the more clustered topologies, which suffer more from neighboring nodes having similar items as message loss increases.

### F. Experimental Evaluation

The experiments in this section simulate the case where a new item  $d$  is introduced by one node in the network in which all caches are full and uniformly populated by  $n = 500$  items. Each experiment takes as input the topology of the network to determine which pairs of nodes can gossip. In all cases, we use a network of  $N = 2500$  nodes arranged in either of the three topologies mentioned in the previous section (a fully connected network, a square grid or a graph where every node has 4 randomly chosen neighbors). In the experiments that follow, after each gossip round, we measure the total number of occurrences of  $d$  in the network (replication), and how many nodes in total have seen  $d$  (coverage).

*Simulations with Shuffle:* Each node in the network has a cache size of  $c = 100$ , and sends  $s = 50$  items when

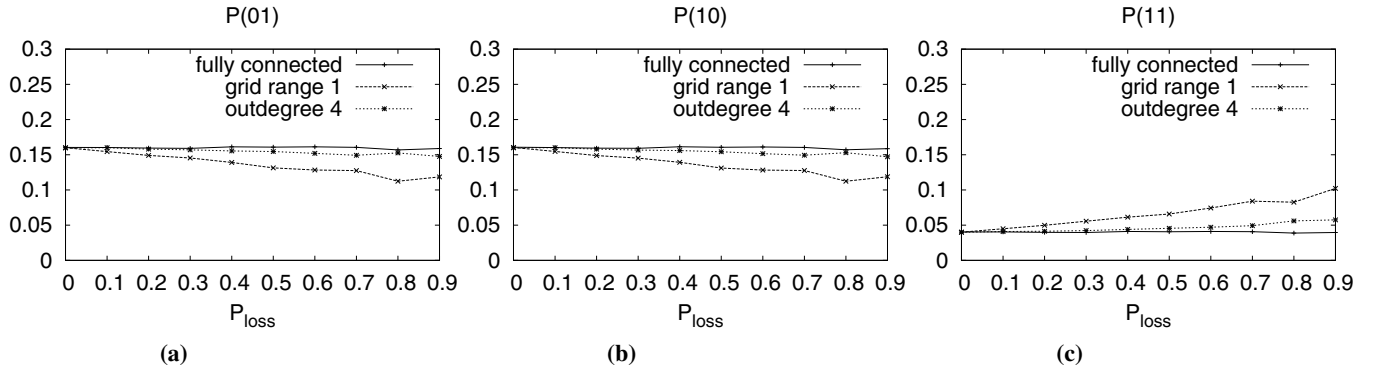


Fig. 9. Probability that a gossip exchange occurs between a) a node that does not have item  $x$  and a node that has the item, b) a node that has item  $x$  and one that does not, and c) two nodes have item  $x$ , for different topologies.

gossiping. In each round, every node randomly selects one of its neighbors and shuffles. For a fair comparison with the simulations with the model, we let the nodes gossip for 1000 rounds with  $P_{loss} = 0$ , to ensure that none of the  $n = 500$  initial items is lost in the startup period before initiating the measurements of the properties. After this startup period, items are replicated and the replicas fill the caches of all nodes. At round 1000,  $P_{loss}$  is set to the desired value and item  $d$  is inserted into the network at a random location. From that moment on, we track its replication and coverage.

*Simulations with the model:* For the simulations with the model,  $n, c$  and  $s$  are system parameters set to 500, 100 and 50, respectively.  $P_{inx}$  is determined experimentally on the network, and  $P_{drop}$  is calculated using equation (2). Instead of maintaining a cache, each node in the network only maintains a variable that represents whether it holds item  $d$  or not (state 1 or 0, respectively). Nodes update their state in pairs according to the transition probabilities introduced before, see Fig. 2. This mimics an actual exchange of items between a pair of nodes according to Shuffle. While in the protocol this results in both nodes updating the contents of their caches, in a

simulation using the analytical model updating the state of a node refers to updating only one variable: whether the node is in possession of item  $d$  or not. At round 0 we set the state of a random node to 1 (while all the others have state 0) and track the state of the nodes for the remainder of the simulation.

Figs 11 and 12 show the behavior of Shuffle (top row) and how it compares to the analytical model (bottom row) in terms of replication (left) and coverage (right) of  $d$ , for different values of  $P_{loss}$ . For each value of  $P_{loss}$ , 100 simulation runs (for both Shuffle and its model) were executed. Due to message loss, it is possible for item  $d$  to disappear after being introduced into the network (usually in the first few rounds). As  $P_{loss}$  increases, this situation is more likely. In the graphs, we only take into account the successful runs, i.e., where the item did not disappear, but spread.

The top rows of Figs 11 and 12 show the average and standard deviation of the successful runs with Shuffle. We compare this data with the average of the successful runs of the model, and present the difference (in absolute value) in the bottom rows of Figs 11 and 12. We include the standard deviation for the shuffle in the bottom row for comparison. It

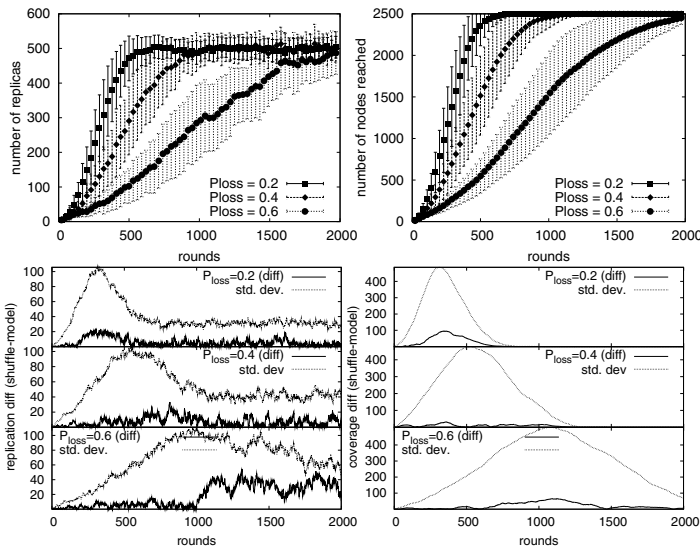


Fig. 11. **Grid, range 1:** Top: Replication (left) and coverage (right) of item  $d$  for the shuffle. Bottom: difference between the shuffle and the model for replication (left) and coverage (right).

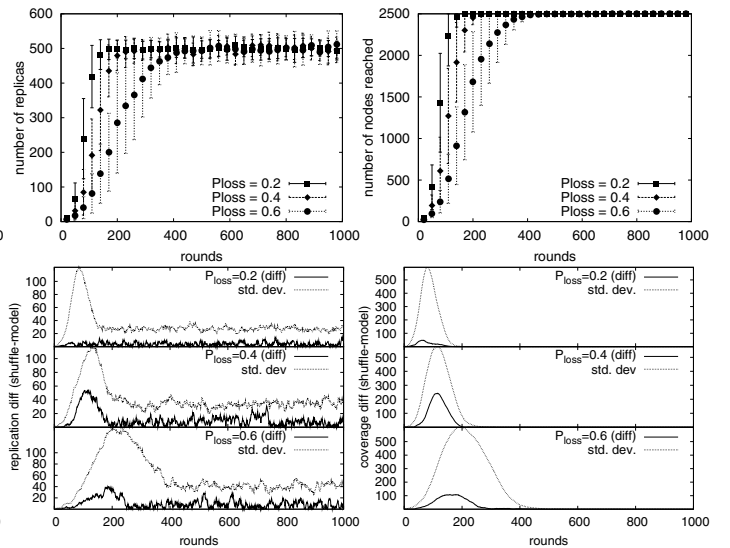


Fig. 12. **Topology with outdegree 4:** Top: Replication (left) and coverage (right) of item  $d$  for the shuffle. Bottom: difference between the shuffle and the model for replication (left) and coverage (right).

clearly shows that the difference between the results obtained from the shuffle and the model fall well within the standard deviation of the shuffle results, confirming the ability of the model in predicting the average behavior of the protocol.

In all successful runs (despite message loss), the network converges to a situation in which there are roughly 500 copies of  $d$ , indicating that after repeated execution of the protocol  $d$  receives a fair share of the storage space in the network;  $2500 \cdot 100$  cache slots divided between 500 items. Also, as expected, due to random gossiping item,  $d$  is eventually seen by all nodes in the network, when coverage reaches 100%.

## VII. BROADENING THE SCOPE: PEER-SAMPLING SERVICE

In the same way that we have developed models for information dissemination algorithms, we can apply our methodology to other types of gossip protocols. In this section, we describe, in broad terms, how to apply our modelling approach to Cyclon, a gossip-based peer-sampling protocol.

### A. The Cyclon Protocol

Peer sampling is a service that nodes in large-scale distributed systems can call to obtain a random peer to gossip with. Cyclon implements a peer sampling service by constructing and maintaining an unstructured overlay using gossiping membership information. As opposed to Shuffle, the data items exchanged by Cyclon are references to other nodes in the network. The references, or links, that a node stores in its cache represent the nodes that it can gossip with. The collection of links in the network constitutes an ever-changing overlay over which links are exchanged. The aim of Cyclon is to keep the caches of the nodes in the network populated with a random selection of links to other nodes. The following table summarizes the protocol:

method	operation
RandomPeer()	Select $s$ random items and place them in $\sigma$ . From $\sigma$ , select a gossip partner uniformly at random.
PrepareMsg()	If the node initiates the exchange, replace the link to the gossip partner with a link to itself in $\sigma$ . Return $\sigma$ .
Update( $\sigma, \sigma_p$ )	Discard links to the node itself and items that are already in the cache from $\sigma_p$ . Include remaining items in cache by 1) using empty slots and 2) replacing entries among the ones in $\sigma$ .

Note that the steps taken within the routines of Cyclon depend on the role that a node has in the gossip exchange. The node that initiates the exchange always includes a link to itself in the message, while the contacted node does not. This is reflected in the PrepareMsg() routine, which is slightly different for the initiator.

### B. Modelling Cyclon: States and Transitions

According to Cyclon, every link  $d$  has a publisher  $D$ , and whenever  $D$  gossips, it sends the link  $d$  to its partner. Thus, when modelling the dissemination of link  $d$  throughout the network, we have to take into account whether  $D$  (the source of link  $d$ ) is involved in the exchange. Therefore, we define the state of a node as a two-bit string, where the first bit indicates whether the node is  $D$  and the second bit indicates whether link  $d$  is in the node's cache (as done in the previous models).

As nodes update their states in pairs, and with each node having a state represented by two bits, the state of a pair of nodes engaged in a Cyclon exchange consists of a four-bit string. While this opens up to the possibility for 16 states, only 8 states are valid. Cyclon precludes a node from storing its own link, eliminating seven states (where one of the nodes has state 11). In addition, the state 1010, where  $D$  contacts itself, is also invalid.

Fig. 13 shows the transitions between states where  $D$  is not involved. For simplicity, we assume that there are no link failures, resulting in a transition diagram similar to the one for Shuffle. Four states depicted have the form 0X0X, indicating that neither the initiator nor the gossip partner is  $D$ .

When  $D$  is involved in the exchange, there are only four possible states, as shown in Fig. 14. Since  $D$  as the initiator always includes a link to itself in the set of items sent, the outcome will always be that the other node has a link  $d$ . On the other hand, when  $D$  is the contacted node (see bottom of figure), the initiator might or might not drop link  $d$  from its cache as a result. In all cases,  $D$  always keeps the state 10, as it can never keep a link to itself in its cache.

Describing the transitions in terms of the building blocks  $P_{select}$  and  $P_{drop}$  can be done in a similar way as with Shuffle (when  $D$  is not involved in the exchange). The variations in the routines, specifically PrepareMsg(), due to the role taken by the node in the exchange, have to be given special consideration, as they will cause  $P_{select}$  to be slightly different for the initiator and the contacted node. When node  $D$  is involved, Cyclon is very clear about the outcome. The transitions can be easily calculated. If node  $D$  is the initiator, there is only one possible outcome (probability = 1). If node  $D$  is the contacted node, the transitions depend solely on  $P_{drop}$ .

### C. Other Protocols

As mentioned before, in the original version of Newscast, data items are timestamped according to their creation time. A node allocates the space in its cache for the received items by discarding corresponding number of oldest items. If an item is received that is also in the node's cache, the recent version of the item is preferred. Like for Cyclon, a state of a transition diagram of Newscast is then a pair of tuples  $(a, b)$ , where  $a, b \in \{0, (1, i)\}$ . The first bit indicates

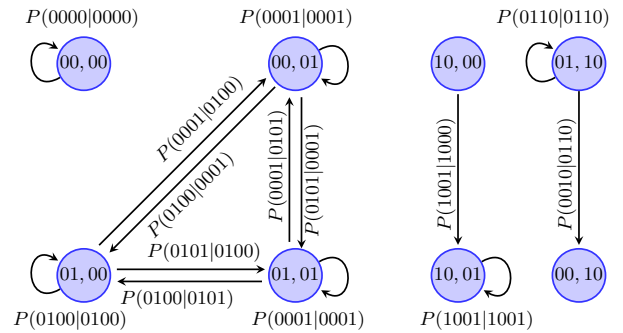


Fig. 13. State transitions when node A and B are not producers of item  $d$ .

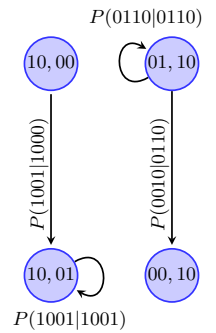


Fig. 14. State transitions when either node A or B is the producer of item  $d$ .

if the data item is present in the gossiping node's cache. The integer  $i$  is a timestamp of the corresponding item. The expression for probability  $P_{select}$  remains the same, but  $P_{drop}$  is then a function of the corresponding timestamp. It can be either derived through rigorous analysis, or can be measured experimentally similar to the approach presented in Sec. VI.

## VIII. CONCLUSIONS

Traditional analysis methods for computer systems such as model checking with its exhaustive state space search, fail to cope with large networks. Although useful for studying certain behavior of small-sized networks, these methods do not scale well for gossip protocols. On the other hand, standard methods for modelling of epidemics scale well, but abstract away the details of a protocol, showing only simple emergent behavior of the system. A challenge is to develop analytical models that capture (part of) the behavior of a system, and then subsequently optimize design parameters, at the right level of abstraction.

In this paper, we presented an analytical framework for a class of gossip-based information dissemination protocols. Modelling a gossip protocol at the level of local pairwise interactions, as demonstrated in this paper, is a scalable approach to analyze such protocols. On the one hand, this analytical model includes the mechanics of communication between nodes on the level of the protocol details. On the other hand, such a model allows for studying the impact of system parameters on the performance of the protocol, and can be used to optimally design and fine-tune it.

Furthermore, we have presented the analysis of a gossip protocol in the presence of transient communication failures. For our framework, we introduced a hybrid method to compute  $P_{drop}$  that combines both rigorous modelling of the protocol and statistical data sampling from large-scale Monte Carlo simulations for different network topologies. To be more precise, we derive analytical expressions for components of our framework that are invariant with respect to the scenarios we want to model. Having decomposed our model into its basic components, we identify the ones that are affected by specific scenario configurations (in this case, message loss and topology combinations). Finding analytical expressions for these components (in this work, only  $P_{inx}$ ) would require modelling each specific scenario configuration, reducing the applicability of the framework to those very specific configurations. Instead, we isolate the framework from the scenario-specific component and use statistical data sampling to obtain a value for it.

We opt for this combined approach since it allows us to build a framework that captures the behavior of the gossip protocol without requiring us to incorporate scenario-specific elements into the model. The challenge in this approach lies in being able to decompose the model into its minimal components, in such a way that the ones which are dependent on particular scenarios (for which expressions that encompass all scenarios cannot be derived) can be isolated and computed

separately. In effect, we strive for a golden mean between high-level models such as for epidemics showing only the emergent behavior and the low-level models of the protocol that depend on particular implementation settings.

With respect to gossip-based dissemination, our study revealed that for networks with lossy communication channels, the assumption of a uniform distribution of data is valid only if every node can gossip with any other node in the network. In future, we plan to study the impact of different gossiping frequencies on the performance results.

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